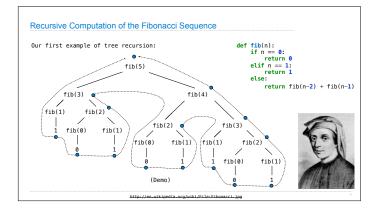
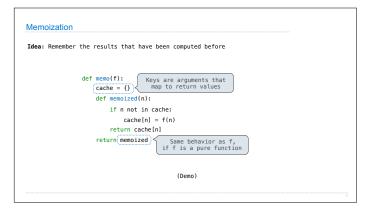
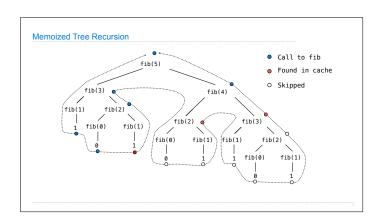


Measuring Efficiency



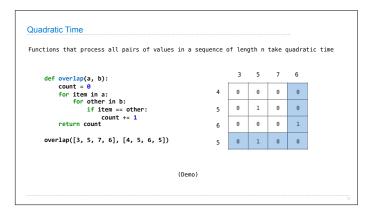
Memoization

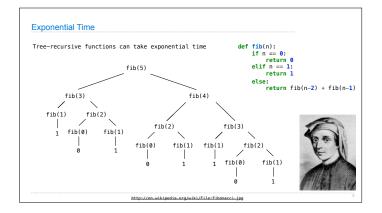


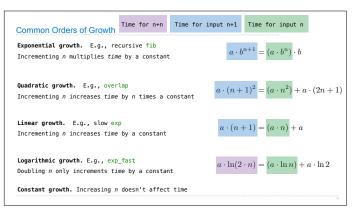


Exponentiation

Orders of Growth







Order of Growth Notation

Exponential growth. E.g., recursive fib	$\Theta(b^n)$	$O(b^n)$
Incrementing $n$ multiplies $time$ by a constant		
Quadratic growth. E.g., overlap	$\Theta(n^2)$	$O(n^2)$
Incrementing $n$ increases $time$ by $n$ times a constant		
Linear growth. E.g., slow exp	$\Theta(n)$	O(n)
Incrementing $n$ increases $time$ by a constant		
Logarithmic growth. E.g., exp_fast	$\Theta(\log n)$	$O(\log n)$
Doubling $n$ only increments $time$ by a constant		
Constant growth. Increasing n doesn't affect time	$\Theta(1)$	O(1)



## Space and Environments Which environment frames do we need to keep during evaluation? At any moment there is a set of active environments Values and frames in active environments consume memory Memory that is used for other values and frames can be recycled Active environments: -Environments for any function calls currently being evaluated -Parent environments of functions named in active environments

(Demo)

