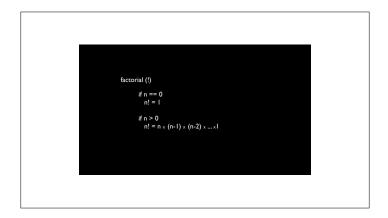
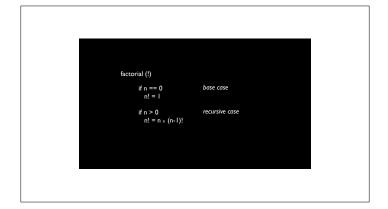
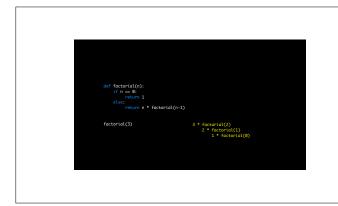


Recursive Factorial







Order of Recursive Calls

```
The Cascade Function
                                                     (Demo)
                                      Global frame
       1 def cascade(n):
                                                                     if n < 10:
print(n)
              else:
                                      f1: cascade [parent=Global]
                 se:
  print(n)
  cascade(n//10)
  print(n)
                                                         n 123
                                      t2: cascade [parent=Global]

    Each cascade frame is from a
different call to cascade.

                                                     n 12
Return
value None
      9 cascade(123)
                                                                     *Until the Return value appears, that call has not completed.
  Any statement can appear before or after the recursive call.
```

```
Two Definitions of Cascade

(Demo)

def cascade(n):
    if n < 10:
        print(n)
        else:
        print(n)
        cascade(n/18)
        print(n)

- If two implementations are equally clear, then shorter is usually better

In this case, the longer implementation is more clear (at least to me)

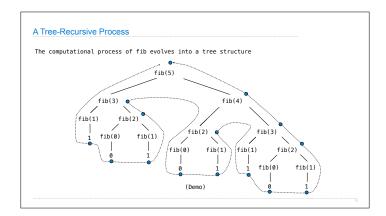
When learning to write recursive functions, put the base cases first

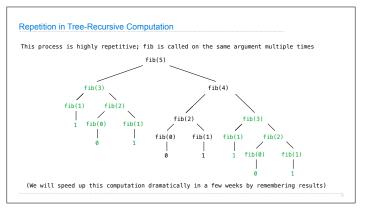
Both are recursive functions, even though only the first has typical structure
```

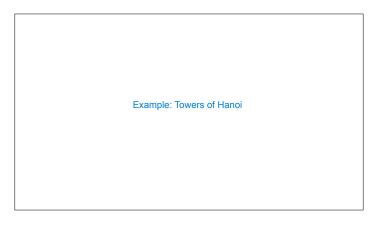
```
Example: Inverse Cascade
```

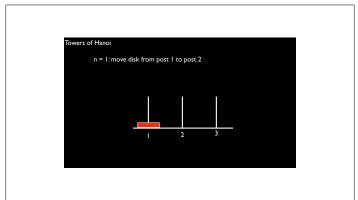
Tree Recursion

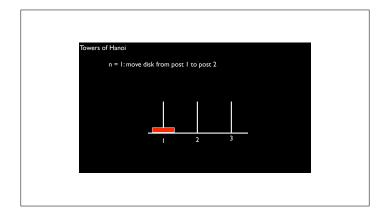
## Tree Recursion Tree-shaped processes arise whenever executing the body of a recursive function makes more than one recursive call n: 0, 1, 2, 3, 4, 5, 6, 7, 8, ..., 35 fib(n): 0, 1, 1, 2, 3, 5, 8, 13, 21, ..., 9,227,465 def fib(n): if n == 0: return 0 elif n == 1: return 1 else: return fib(n-2) + fib(n-1)

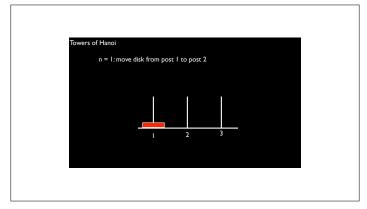




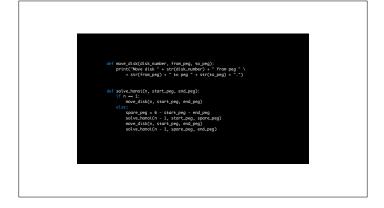


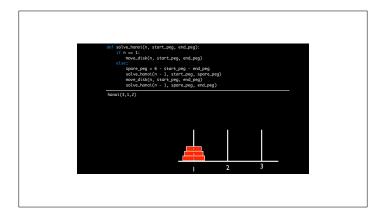














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